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Investigation of fracture intersection behaviors in three-dimensional space based on CT scanning experiments

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Abstract: The generation of a fracture network in reservoir rocks for fluids to flow via hydraulic fracturing is important in shale oil and gas development, and the intersection between hydraulic and natural fractures is key in bridging natural fractures. In this work, the intersection behaviors between hydraulic and natural fractures and fracture propagation in a three-dimensional (3D) space were investigated. A hydraulic fracturing lab facility is designed and a series of fracturing tests on eight underground cores from the Kong shale reservoir are carried out. First, visualization analysis was conducted on each sample before and after fracturing with the assistance of an X-ray CT scan and the following up 3D reconstruction. Second, an extension model of fracture intersection between natural and hydraulic fractures is established in 3D through analytical calculations. Finally, the intersection behaviors are classified into six zones according to our model analysis. Apart from interesting results and findings, insights into the formation and propagation of fracture networks are also provided, which are of great value in characterizing shale reservoirs.

Keywords: fracture intersection, intersection criteria, true triaxial experiment, fracture propagation, X-ray CT scan

Abbreviations

3D	Three-dimensional
CT	Computerized tomography
HF _s	Hydraulic fractures
NF _s	Natural fractures
2D	Two-dimensional
DA	Dip angle
AA	Azimuth angle

List of symbols

34	τ_0	Shear stresses of natural fracture
35	K_f	Coefficient of friction
36	T	Shear stresses acting on NF
37	σ_n	Normal stresses acting on NF
38	p_0	Pore pressure imposed on the NF surface
39	σ_1	Maximum in-situ principle stress
40	σ_3	Minimum in-situ principle stress
41	p_σ	Treatment overpressure
42	T_0	Tensile stress
43	b	Coefficient
44	σ_{H1}	Stress along the HF plane and is perpendicular to the intersection line
45	σ_{v1}	Stress along the HF plane and the intersecting line

46 1. Introduction

47 Hydraulic fracturing has become a key stimulation technique to enhance the productivity in shale oil
48 and gas reservoirs. Owing to the extremely low permeability and dominant pores at nano-scale, the major
49 role of hydraulic fracturing is to generate connections among natural fractures, resulting in flow channels to
50 be created and the distance of oil and gas seepage being reduced, which consequently produces a large
51 stimulation reservoir volume (Zhang et al. 2018; Zhang and Sheng 2020). The fractures created by
52 hydraulic fracturing are complex and form a fracture network for fluid to flow through (Fan and Zhang
53 2014; Hou et al. 2016). The intersection between hydraulic fractures (HFs) and natural fractures (NFs)
54 during fracturing plays a key role in forming the fracture network (Hou et al. 2016; Rueda et al. 2020).
55 Particularly, Gale et al. (2007) have investigated the importance of NFs in hydraulic fracturing treatments.
56 When HFs meet NFs, the HFs will pass through, turn along NFs, or be arrested by NFs (Rueda et al. 2020;
57 Kolawole and Ispas 2020; Janiszewski et al. 2019). Hence, it is important to understand the mechanisms of
58 creating a complex fracture network in naturally fractured shale reservoirs.

59 Laboratory scale true triaxial hydraulic fracturing test is a popular approach to directly investigate
60 fracture propagation behaviors during reservoir stimulation. There are several experimental studies on the
61 intersection between HFs and NFs (Warpinski et al. 1982; Ruxin et al. 2019; Zou et al. 2016). Meanwhile,
62 various visualization techniques have been adopted to monitor fracture propagation paths in rock samples,
63 such as splitting artificial or outcrop rocks (Zou et al. 2016, Zhi et al. 2015), using acoustic emission and
64 microseismic data to analyze fracture geometry (Bennour et al. 2015, Ma et al. 2017), adding tracers into
65 fracturing fluid to track fracture extension in rock samples (Fu et al. 2016, Tan et al. 2020). These studies
66 analyzed the impact of intersection angle, stress difference, fracturing fluid viscosity, and fracturing
67 engineering parameters on fracture propagation, but neglected the effect of dip angle, which broadly exist
68 in NFs in the formations (Gale et al. 2014). Following up, Dehghan et al. (2015) investigated the influence
69 of the dip angle and azimuth on fracture propagation through performing splitting rock sample experiments.
70 In addition, Heng et al. (2019) considered crack propagation with various dip angles via numerical
71 simulation based on an acoustic emission monitoring experiment.

72 Over the past decades, as a non-destructive technique, X-ray computed tomography has been widely
73 employed for the characterization of fracture propagation. Zou et al. (2016) analyzed the influence of field
74 treatment and geological parameters on fracture propagation with partially opened bedding planes and
75 provided suggestions on how to create complex fracture networks in shale formations. He et al. (2016)
76 compared hydraulic fracture extension patterns in fractured shale, sandstone, and granite cores, and
77 demonstrated the impact of bedding planes early developed in shale on fracture morphology. Guo et al.
78 (2014) investigated the impact factors of stimulated shale reservoir volume by the high-energy CT scanning
79 technique. Zou et al. (2016) studied the hydraulic fracture propagation in natural bedding using CT
80 technology. However, the majority merely mention the plane expansion morphology of fractures because of
81 the lack of three-dimensional (3D) reconstruction of fracture voids. Jiang et al. (2019) and Luo et al. (2019)
82 used 3D reconstruction for analyzing fracture propagation morphology, nevertheless, they did not consider

83 the interaction between HF and NFs.

84 To understand the intersection behaviors, many scholars have conducted several theoretical studies.
85 Zhuang et al. (2020) and Zheng et al. (2019) established a numerical model to analyze the intersection
86 between HF and NF. Warpinski and Teufel (1987) proposed an analytical model to estimate whether NF
87 will be dilated or fail in shear slippage due to approaching HF. Based on linear elastic mechanics,
88 Renshaw and Pollard (1995) had established across criterion for hydraulic fracture intersection with an
89 orthogonal discontinuity. Gu et al. (2012) extended the criterion to the non-orthogonal interface. Fu et al.
90 (2018) developed a new 3D analytical criterion to quantify the dependence of natural fracture tensile/shear
91 failures on the properties of spatially-varied NFs, including the proportion of cemented region(s), natural
92 fracture height, and cementation strength. Recently, Blanton (1986) created a model of HF penetrating
93 NFs with good agreement compared with experimental results.

94 In this study, several underground cores of the second Kong shale reservoir were used to prepare
95 square-shaped samples for true triaxial fracturing experiments. Before the respective experiments, CT
96 scanning and subsequent 3D reconstruction were used to characterize the spatial distribution of NFs. At the
97 end of every test, CT scanning and 3D reconstruction are invoked again to expose the resultant fracture
98 network after hydraulic fracturing, viewing and quantify fracture extension in terms of morphological
99 properties and flow behaviors. Furthermore, an intersection extension model between HF and NF in 3D is
100 established and an assessment chart is generated to distinguish various intersection extension zones for the
101 second Kong shale reservoir.

102 2. Experiments

103 2.1 Specimen preparation

104 Eight core samples were taken from several wells located at shale oil reservoirs at depths between
105 2800 and 4200 m in Cangdong Sag, Bohai Bay Basin, China. The cylindrical cores have an identical
106 diameter (100 mm) and length (95 mm). The measured porosities and permeabilities range from 5.09% to
107 10.51% and from 0.44 to 6.84 mD, respectively. Among all samples, Yong's modulus is 17,743 MPa, and
108 Poisson's ratio is 0.267, on average. Regarding the triaxial hydraulic fracturing involved in our experiment,
109 as shown in Fig.1(a), each original sample needs to be wrapped up with filling materials to make a
110 cuboid-shaped sample of three dimensions of 105 mm × 105 mm × 95 mm, which is the same dimension as
111 the true triaxial hydraulic fracturing testing holder. The filling materials are composed mainly of G-grade
112 cement, water, and sand (60 mesh), made with a sand cement ratio of 1.8:1, and has similar properties as
113 the core themselves (Table 1), which were used as core specimens.

114 A wellbore shown in Fig. 1 is located in the middle of each core sample with a steel case coupled with
115 an open-hole section. The steel case has 20 mm in length, 10 mm in exterior diameter, and 8 mm in interior
116 diameter, was glued in place by an epoxy adhesive, which generated a bonding strength several times
117 greater than the tensile strength of the rock specimens.

118 2.3 Fracturing equipment

119 The true triaxial fracturing system shown in Fig. 2 was set up to perform our hydraulic fracturing tests
120 with a loading capacity of 20 MPa in three orthogonal directions. To avoid unbalanced loading at
121 boundaries, the maximum horizontal stress (σ_H), minimum horizontal stress (σ_h) and vertical stress (σ_v)
122 were simultaneously applied incrementally but slowly on the specimen until a targeted value to be reached.
123 During testing, rock specimens were first fractured under high hydraulic pressures. At the end of fracturing,
124 i.e., stopping pumping water, the confining stresses were maintained for a couple of minutes until the
125 generated tensile fractures are closed tightly. Over that duration, rock samples were then taken out for CT
126 scanning.

127 2.4 Natural fracture before fracturing

128 A computer was used throughout the whole test procedure to control and monitor the experiments and
129 collect data. A micro-CT scanning system was used to characterize the spatial distribution of NFs before
130 pumping water and to capture the propagation of HFes at the end of water pumping. The system consists of
131 an acquisition computer, a reconstruction computer, and a shielded cabinet that includes a 240-kV
132 micro-focus X-ray tube, an X-ray detector array, and a rotatable sample holder. The two-dimensional (2D)
133 cross-sectional images acquired by CT scanner (Luo et al. 2019) were further reconstructed into 3D images,
134 which are obtained using a commercial software called VGStudio, to reveal the spatial distribution of
135 fracture opening voids in rock samples.

136 The number, density, spreading direction, and angle of NFs in rock samples can be captured by CT
137 scanning with fracture recognition software. To facilitate the observation of the spatial geometry of
138 fractures, rock samples were sliced in three directions: facing up, side-looking, and overlooking, as shown
139 in Fig. 3(a). Y-direction links to the " σ_H " direction, and X direction to the " σ_h " direction, as shown in Fig.
140 3(b). The dip angle (DA) and the azimuth angle (AA) of fractures are two key parameters, as shown in Fig.
141 3.

142 2.5 Experiment design

143 The in-situ horizontal stress difference ($\sigma_H - \sigma_h$) and intersection angle are the predominant elements
144 (Gu et al. 2012; Yao et al. 2018) in fractures intersection. So, in our experiments, we maintained the vertical
145 press σ_v at 16 Mpa while allowed the in-situ stress difference to change for evaluating the influence of the
146 two factors. Table 2 lists the eight samples and the properties concerned with our experiments. Horizontal
147 stress difference is set as one of four values: 0, 0.5, 2, and 4 MPa. The vertical stress difference (i.e., the
148 difference between vertical and horizontal minimum stress) is set as one of four values: 5, 7.5, 10, and 15
149 MPa. For integrity, lick water of the viscosity of 5 CP was used as fracturing fluid, and a single pumping
150 rate of 12 mL/min is fixed in every test.

151 3. Observations and results

152 3.1 3D visualization

153 Fig. 4 shows 3D fractures in eight samples before and after the hydraulic fracturing. Among all

154 original samples, only samples 25–1 have no NFs, and the rest mainly contain horizontal NFs. Table 3 lists
155 the dip and azimuth angles of NFs with interactive relationships before fracturing. Note that the measured
156 angles may not be that accurate due to the difficult identification in discrete space. Apart from this
157 observation, this paper analyze fracture intersection and propagation in Section 3.2 and further conduct an
158 in-depth mathematical derivation of the interactive propagation of HF and NFs in 3D in Section 4.

159 Shale is usually considered a transversely isotropic material in the experiment and theory ([Sinha et al.](#)
160 [2006](#), [Valente et al. 2012](#)), and there are discontinuous structural planes such as bedding and NFs in shale.
161 The direction of fracture propagation is affected by discontinuous structural planes ([Jiang et al. 2019](#)), thus
162 forming a complex fracture network. This phenomenon is observed in Fig. 4 (b) - (h).

163 3.2 Fracture propagation analysis

164 3.2.1 Samples with two symmetric wing fractures

165 New NFs were created in the shale matrix, and HF was extended toward horizontal maximum
166 principal stress, without intersection with NFs to be observed, forming a single HF, so it suggests that
167 fracture propagation is mainly controlled by in-situ stress. Such a phenomenon was found in sample 30 as
168 well.

169 Sample 30 does not have NFs but has only one vertical symmetrical biplane fracture (see HF1 in Fig.
170 4(a)) generated under the horizontal stress difference of 0.5 MPa, indicating that complex fractures are
171 difficult to form in the shale, even with the low-stress difference if there is no original NFs.

172 3.2.2 Hydraulic fracture extension

173 As there are NFs near or even directly connected to the wellbore, it is well-recognized that generating
174 new HF is rare in the rock matrix during fracturing, however, existing NFs can be opened and extended
175 further. The fracture propagation within such sample is controlled by NFs, which is confirmed in
176 experiments with samples 31, 34, and 25–1 too.

177 There are four NFs in sample 31. NF1, NF2, NF3, and NF4 are well connected to the wellbore, and
178 consequently, no new HF is generated through fracturing, instead, the four fractures are extended to some
179 extent along with their original directions (Fig. 4 (c)).

180 There are three NFs in sample 34. As NF1 and NF2 are connected to the wellbore, HF spread along
181 with these two fractures during fracturing (Fig. 4 (e)). However, NF3 is connected to neither the wellbore,
182 nor NF1 and NF2, and thus no new HF can be generated in the experiment.

183 Five inter-connected NFs can be found in samples 25–1. As NF1, NF3 and NF4 are connected to the
184 wellbore, and NF1 is intersected with both NF2 and NF5, the originally existing NFs spread along with
185 these five fractures during fracturing (Fig. 4(f)). However, no new HF was generated consequently.

186 3.2.3 Intersection between HF and NFs

187 From these experiments, it can be observed that HF can be created in the shale and be extended to
188 intersect NFs. In addition, HF can also cut through NFs or cause NFs to shear, slip, and spread along with
189 natural fractures. As illustrated in Fig. 4 for samples 33–2, 25–2, 26, and 28, it is evident that fracture

190 propagation is controlled by stress and NFs.

191 Four separated NFs exists in sample 33–2 (Fig. 4(d)). During hydraulic fracturing, two new vertical
192 HF1 and HF2 are generated, indicating that complex fractures are likely to occur if the stress difference is 0.
193 HF1 intersects NF2 at 48.5° upwards and NF3 at 35.6° downwards, causing them to shear slip and spread
194 along with the NFs. HF2 intersects both NF2 and NF3 vertically and turns along with them. NF1 and NF4
195 are not connected as HF does not penetrate the NF. Limited by the view angle, this phenomenon may not be
196 that clear to be seen in Fig. 4 but can be confirmed by observing the post-fractured rock sample in Fig. 5.

197 In sample 25–2 exists only one NF. Hydraulic fracturing triggers a new vertical HF1 along the
198 direction of maximum horizontal stress and spread downwards and penetrate NF1 (Fig. 4(b)).

199 With two NFs in sample 26, hydraulic fracturing results in a new vertical HF1 that is parallel to the
200 maximum horizontal stress. HF1 spreads with a higher aperture and cuts through NF2. The connection of
201 NF2 with NF1 forces NF2 to spread upwards and open NF1 up (Fig. 4(g)).

202 There is no NFs near the wellbore although four NFs exist in sample 28, as a result, a new two
203 symmetrical wing vertical fracture, HF1, is generated on the upper region of the sample along the direction
204 of the maximum stress, which causes shear slip on NF1 (Fig. 4 (h)). As the HF is parallel to NF1, NF3 and
205 NF4 are at the bottom regions of the rock sample. It can be observed that the new fracture is not connected
206 with any of NF2, NF3, and NF4.

207 3.2.4 Insights into fracture propagation

208 The experimental results show that NFs have a big influence on fracture propagation and play a key
209 role in the creation of complex fractures. If NFs do exist in rock samples, complex fractures are more likely
210 to form after hydraulic fracturing.

211 (1) If NFs are not connected to the wellbore, new HFs can be created by fracturing, and the generation
212 of new HFs are mainly controlled by stress and can expand along the direction of maximum horizontal
213 stress.

214 (2) If NFs are connected or close to the wellbore, HFs are hardly generated. Instead, NFs can be
215 opened up and even be extended further.

216 (3) If the intersection angle between HFs and NFs is small, newly-created HFs tend to spread along
217 with NFs, as seen in samples 33–2. If the intersection angle is large, HFs are ready to cut through NFs, as
218 seen in samples 26 and 25–2. This observation is consistent with the finding by Zhao et al. (2019).

219 (4) Due to the influence of natural fracture DA, the stress state of both HFs and NFs is unclear in 3D
220 space, so the influence analysis of ground stress difference cannot be conducted effectively. Therefore, it is
221 necessary to conduct further fracture propagation analysis in three-dimensional space.

222 4 Theoretical analysis of interaction behaviors

223 Through our experiments, the intersection behaviors of fractures were analyzed as described above.
224 Fracture intersection is a collective result from various elements, such as ground stress, intersection angle,
225 rock mechanics parameter, and fluid pressure in fracture.

226 4.1 Slippage and opening criterion

227 Fig. 6 shows a two-dimensional schematic of HF intersecting NF, which is a simplified diagram if the
228 DAs are set to be 90°. For creating shear slippage in NFs, the condition can be found in (Luo et al. 2019;
229 Warpinski and Teufel 1987) as:

$$230 \quad |\tau| > \tau_0 + k_f(\sigma_n - p_0). \quad (1)$$

231 where τ_0 is the shear stress of natural fracture, K_f is the coefficient of friction, τ and σ_n are the shear
232 and normal stresses acting on NF, respectively, p_0 is the pore pressure imposed on the NF surface.

233 Let the intersection angle between HF and NF in Fig. 6 is denoted by θ ($0 < \theta \leq \pi/2$), the shear stress,
234 and normal stress acting on the plane of a natural fracture can then be obtained according to the 2D stress
235 resolution in [Renshaw and Pollard 1995] as:

$$236 \quad \tau = \frac{\sigma_1 - \sigma_3}{2} \sin 2\theta, \quad (2)$$

$$237 \quad \sigma_n = \frac{\sigma_1 + \sigma_3}{2} + \frac{\sigma_1 - \sigma_3}{2} \cos 2\theta. \quad (3)$$

238 where σ_1 is the maximum in-situ principle stress, σ_3 is the minimum in-situ principle stress.

239 From Warpinski and Teufel [Warpinski and Teufel 1987], if HF intersects NF, the tip can be blunted
240 and the pressure at the intersection can be given by:

$$241 \quad p_0 = p_\sigma + \sigma_3, \quad (4)$$

242 where p_σ is the treatment overpressure. Substituting Eqs. (2), (3) and (4) into Eq. (1), the criterion for
243 shear slippage can be described by Eq. (5),

$$244 \quad (\sigma_1 - \sigma_3) > \frac{2\tau_0 - 2p_0 k_f}{\sin(2\theta) - k_f + k_f \cos(2\theta)}, \quad (5)$$

245 and the criterion for natural fracture opening is simplified as:

$$246 \quad p_0 > \sigma_3, \quad (6)$$

247 further, substituting Eqs. (3) and (4) into Eq. (6) gives

$$248 \quad (\sigma_1 - \sigma_3) < \frac{2p_\sigma}{1 - \cos(2\theta)}. \quad (7)$$

249 4.2 Crossing criterion

250 Based on the elastic solution of stress in the interaction zone and assumes that the initial interaction for
251 HF is to be blunted by the pre-existing NFs. Fracture crossing might occur if the stress difference, $\sigma_1 - \sigma_3$,
252 exceeds the pressure required by Blanton [Blanton 1986] as:

$$253 \quad \sigma_1 - \sigma_3 > -\frac{T_0}{\cos 2\theta - b \sin 2\theta}. \quad (8)$$

254 where T_0 is the tensile stress, b is a coefficient, and $b = 0.2$ in this work, which is determined by frictional
255 slippage along the natural fracture and geometry of the interaction zone.

256 4.3 Stress distribution in 3D

257 As shown in Fig. 6, it is worth emphasizing that the interacting criteria presented above are established

258 based on the fracture configuration in 2D. In our experiment, however, HFs and NFs are considered in 3D,
 259 as shown in Fig. 7, which indicates that the stress distribution in 3D is distinct from the counterpart in 2D.
 260 Hence, it is necessary to re-establish the stress distribution state of the cross-sections perpendicular to HFs
 261 and NFs, so that the stress state can meet the conditions of the previously established 2D model (Eqs. (5),
 262 (7), and (8)).

263 Fig. 7 demonstrates a common scenario of HFs intersecting NFs, where typical HFs are vertically
 264 inclined with a DA of 90° and in a direction that is parallel to the maximum principal stress. The NF has a
 265 DA of α and an angle of θ between the fracture plane and the maximum horizontal stress. σ_v is the
 266 vertical stress, σ_H is the maximum horizontal stress, and σ_h is the minimum horizontal stress. The red line
 267 in Fig. 7 stands for the intersection between HF and NF, on which the three stress values σ_{H1} , σ_{v1} and σ_h
 268 can be pinpointed as the distribution shown in Fig. 8. σ_{H1} is perpendicular to the intersecting line and
 269 passes through the natural fracture along the direction of the hydraulic fracture. σ_{v1} is along the
 270 intersecting line and σ_h is perpendicular to the hydraulic fracture plane. The plane determined by σ_{H1}
 271 and σ_h is perpendicular to both the HF and NF. This surface is the 2D plane in which the 3D space stress
 272 field is transformed into the 2D plane stress field. It is similar to the 2D plane stress field in Figure 6.
 273 Therefore, when σ_{H1} is obtained, the 2D fracture interaction model established above can be used for
 274 calculation.

275 Fig. 8 is a 2D diagram of stress distribution along the hydraulic fracture plane on the intersection line
 276 under the action of maximum principal stress, minimum principal stress, and natural fracture DA.
 277 According to the elastic mechanic's theory [Zhao et al. 2019], σ_{H1} and σ_{v1} can be obtained by:

$$278 \quad \sigma_{H1} = \frac{\sigma_v + \sigma_H}{2} + \frac{\sigma_v - \sigma_H}{2} \cos 2\alpha, \quad (9)$$

$$279 \quad \sigma_{v1} = \frac{\sigma_v + \sigma_H}{2} - \frac{\sigma_v - \sigma_H}{2} \cos 2\alpha. \quad (10)$$

280 where σ_{H1} is the stress along the HF plane and is perpendicular to the intersection line, σ_{v1} is the stress
 281 along the HF plane and the intersecting line. Therefore, comparing with the stresses in Fig. 7, The
 282 maximum and minimum in-situ principle stresses respectively are:

$$283 \quad \sigma_1 = \sigma_{H1}, \quad \sigma_3 = \sigma_h. \quad (11)$$

284 let σ_H , σ_H and σ_h be 16, 10, and 6 MPa, respectively. The stress difference (Fig. 9) as a function of DA
 285 can be calculated using Eq. (11). Note that the DA has a significant influence on the stress difference. With
 286 the decrease in the DA, the stress difference increases accordingly. This is because as the dip angle
 287 decreases, the horizontal maximum stress gradually approaches the vertical stress (see Fig. 7).

288 3.3.4 Intersection behaviors

289 In our experiments, the intersections between newly-created HFs and original NFs were found only in
 290 four samples, i.e., 25–2, 33–2, 26, and 28. With the established model (Eq. (11)), Table 4 gives the detailed
 291 results of various intersections between HFs and NFs.

292 Mechanical strength tests of Kong shale show that the average value of tensile stress of rock, T_0 , is
 293 3.0 MPa, cohesion strength is 1.5 MPa, and the coefficient of friction, K_f , is 0.6, and the average treatment
 294 overpressure is 2.0 MPa. Combining the slippage, opening, and crossing criteria expressed in Eqs. (5), (7),

295 and (8), a mapping can be created to mathematically predict the interaction behaviors with a module of
296 computer codes. As a result, the corresponding critical slippage, opening, and crossing curves can be drawn
297 on an angle-stress coordinate system as delineated in Fig. 10, which is also confirmed by our experimental
298 results (dots and stars) to some extent.

299 Fig. 10 illustrates the intersection behaviors (e.g., slippage, opening, and crossing) between HFs and
300 NFs for both intersection angle and in-situ stress, which may be subjective to the mechanical parameters of
301 Kong shale though. The slippage, opening, and crossing curves are calculated according to Eqs. (5), (7),
302 and (8), respectively. The shear (see blue dots in Fig. 10) and penetration (see the red stars in Fig. 10) of
303 NFs in our experiments (see Table 4) agree well with our calculated results. Moreover, the intersection
304 behaviors can be divided into six possible zones (represented by different colors in Fig. 10).

305 (1) Crossing zone: HFs directly penetrate NFs.

306 (2) Slippage and opening zone: Shear slippage and opening occurred in NFs and HFs could be
307 extended along with NFs.

308 (3) Opening zone: NFs are opened wider and HFs can be extended along with NFs.

309 (4) Slippage zone: Shear slippage occurs in NFs, and HFs can spread along with NFs.

310 (5) Slippage and crossing zone: Upon the impact of hydraulic fracture tip stress and far-field in-situ
311 stress, HFs can expand and cut through NFs. After the fluid enters NFs, shear slippage can occur in NFs.

312 (6) Arrested zone: No slippage or opening occurs in NFs, besides HFs cannot cut through NFs.

313 For the Kong shale oil reservoir, therefore, three predictions can be made: (a) if the intersection angle
314 ranges from 0° to 4° , NFs might open up; (b) if the intersection angle is between 4° and 56° , shear slippage
315 might occur; (c) if the intersection angle is greater than 56° , HFs likely cut through NFs.

316 5 Conclusions

317 (1) Hydraulic fracturing experiments on underground shale rock samples were conducted in a true
318 triaxial fracturing system and examined visually and analytically before and after testing. The 3D images of
319 the original samples before hydraulic fracturing shows that NFs can occur at different angles and dips.

320 (2) NFs and stresses are two controlling factors for fracture propagation. If NFs are not connected to a
321 wellbore, fracturing can create HFs, which are determined by stress that further forces the new HFs to
322 propagate along the direction of maximum horizontal stress. If the extended fracture intersects NFs, the
323 intersection behaviors are then dictated by both stress difference and the morphology of NFs. If NFs are
324 connected to or very close to a wellbore, HFs can be hardly generated, and HFs can expand only along with
325 NFs even though HFs do occur.

326 (3) The intersection angle, DA, and stress difference are the key factors to intersection behaviors
327 between hydraulic and NFs. If the intersection angle is small, the DA is large, and the stress differences are
328 low, the resultant HFs tend to spread along with NFs. If the intersection angle is large, the DA is small, and
329 the horizontal stress difference is high, the created HFs more likely to penetrate NFs.

330 (4) If an intersection between hydraulic and NFs occurs, the hydraulic fracture can force the natural
331 fracture to open up wider, leading NFs to slip and even to be captured by HFs. According to the opening

332 boundary, slippage boundary, and crossing boundary curves calculated from our models, the intersecting
333 behaviors can be divided into six zones: crossing zone, slippage and opening zone, opening zone, slippage
334 and crossing zone, slippage zone and arrested zone, which can be employed as a tool to characterize shale
335 reservoirs effectively.

336

337 Founding

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339 Compliance with Ethical Standards

340 Conflict of interest: The authors declare that there is no conflict of interest.

341

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