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# Use of Optimized Centroid and Weighted Centroid Algorithms to Locate a Partial Discharge Source by Using Received Signal Strength

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**Abstract**—Received signal strength (RSS) based localization of a source is a simple but effective technique. In RSS based localization source location is estimated by converting obtained signal into distance. In this paper, centroid and weighted centroid algorithms has been utilized to locate a partial discharge (PD) source. An artificial PD signal was generated, and signals were captured using radio frequency (RF) sensors and hence the location of the source was estimated. The location of the source was estimated for three different positions. There were eight measurement sensors used and received signal was converted into dBm as input to the location algorithm.

**Keywords** — RSS; centroid; partial discharge; sensors.

## I. INTRODUCTION

In high voltage systems (HV), PD is a phenomenon that partially bridges conductors. PD, if left unattended, will lead to catastrophic failures resulting in economic and human losses [1, 2]. Equipment such as switchgears, power generators and transformers and power cable are mainly prone to PD [3-5]. Generally, PD takes place due to insulation cracks that cause treeing between the insulation material and the conductors [5, 6].

A range of algorithms have been implemented in the past to estimate the location of PD in HV systems. These algorithms include time of arrival (TOA), time difference of arrival (TDOA), angle of arrival (AOA), use of SDR, USRP and difference of arrival [3, 7, 8]. Algorithms such as TOA, TDOA, AOA and DOA are all based on the localization of PD sources based on real PD pulses [9-11]. This brings the need for time based receiver node synchronization [12, 13].

For one off measurement and localization of PD, such algorithms are useful, however, for continuous monitoring, these time based algorithms are not plausible due to two main reasons [11, 14, 15]. Firstly, the requirement of nodes synchronization brings the need for expensive hardware and software solutions. Especially for synchronization, there will be a need of expensive clock. The second main reason is the scalability challenge [16]. In such algorithms, if the scope of the problem gets bigger, it will become a challenge to add additional receiving nodes in the existing system in place [17-19].

Considering these factors, the RSS based centroid and weighted centroid algorithms have been explored to locate the

position of a PD source. The main advantage of using RSS is that, it works on the received energy rather than the real pulse itself [20]. The nodes synchronization does not remain an issue anymore due to lack of dependency on time constrained PD pulse itself. The second advantage is that in RSS based localization, the scalability is not an issue. Additional receiving nodes can be included with the system in place, should the scope of the problem gets bigger due to bigger coverage area.

## II. PROBLEM DESCRIPTION

Partial discharge has been the topic for researchers in the past three decades. Power companies are fully aware of the phenomenon and have the systems in place to assess the condition of high voltage systems such as transformers. A common method to assess the conditions of HV systems by the power companies is to use a hand held device outside HV transformers every few months. Continuous monitoring of PD has not yet been deployed mainly due to techniques being less feasible to be deployed for continuous monitoring. Enhancements in the communication technology over the past two decades have led researchers to focus on the techniques that can be deployed for continuous monitoring of PD [21-24]. Based on this, existing centroid and weighted centroid algorithm are utilized to locate PD source. The main challenge while locating a PD source is that the location of the source is unknown as well as the source transmitted power.

The algorithm described in [25] uses the received signal and estimates the centroid based location of the source by using the received signal. The algorithm utilizes the path loss model equation, as shown in equation (1):

$$PL(d_0) = 32.44 + 10n\log(d_0) + 10n\log(f) \quad (1)$$

Where  $PL(d_0)$  is the path loss of the radio signal transmitted at distance  $d_0$ , while  $d_0$  is the distance of the reference node,  $n$  is the path loss coefficient of the environment (1 to 5), and  $f$  is the transmitted signal frequency.

## III. DESCRIPTION OF ALGORITHM

Employing the log-normal distribution model which takes into consideration the path loss of the reference node, and the distance of the respective receiver nodes, the path loss model equation (1) can be expressed as:

$$PL(d) = PL(d_0) + 10n\log(d_0) + \vartheta \quad (2)$$

Where  $PL(d)$  is the radio signal path loss transmitted over the distance  $d$ ,  $\vartheta$  is the Gaussian random variable having average of zero with a range of standard deviation.

The received signal strength (RSS) can be determined as:

$$RSSI = P_{send} + P_{amp} - PL(d) \quad (3)$$

Where RSS is the received signal strength,  $P_{send}$  is the transmitting power and  $P_{amp}$  is the antenna gain.

Having conducted measurements of the RSS for three different node locations, the actual transmitter location coordinates was recorded and then the centroid and weight centroid algorithms were applied to determine the estimated location of the transmitter for each case.

The conventional centroid algorithm does not take into consideration the receiver node placed at the centroid location. Also the accuracy of the common centroid algorithm is affected. Therefore, there was the need to develop an optimized centroid algorithm. As described in , the method used to determine the location of the unknown transmitted locations for the measurement results obtained is based on trilateration method. The three receiver location nodes  $A(x_A, y_A)$ ,  $B(x_B, y_B)$ ,  $C(x_C, y_C)$  are optimally selected based on the measurement RSS. Below are the key steps for the optimised centroid algorithm:

a) Assuming that the shadow effect in equation (2) is 0 then the distances from the receiver nodes to the unknown nodes can be determined as:

$$d = 10^{\left(\frac{RSSI}{10n}\right)} \quad (4)$$

b) Based on the computed distances in equation (4), rank the distances and select the three least distances from the unknown received nodes to the estimated transmitter location. The calculated ranked distances  $d_A$ ,  $d_B$  and  $d_C$  are then used to determine the unknown transmitter location.

Using trilateration method, the distances obtained can be defined as:

$$d_A = \sqrt{(x - x_A)^2 + (y - y_A)^2} \quad (5)$$

$$d_B = \sqrt{(x - x_B)^2 + (y - y_B)^2} \quad (6)$$

$$d_C = \sqrt{(x - x_C)^2 + (y - y_C)^2} \quad (7)$$

c) The equations (5) to (7) have two unknowns, hence a combination of the equations is solved simultaneously to obtain the estimated transmitter location  $x_1$ ,  $x_2$  and  $x_3$ . Also using the trilateration algorithm, the Centre of the triangle formed by the three anchor receiver nodes is obtained easily as used as the fourth estimated  $x_4$ .

d) The optimized estimated location is then determined using centroid algorithm as follows:

$$x = \frac{x_1 + x_2 + x_3 + x_4}{4} \quad (8)$$

$$y = \frac{y_1 + y_2 + y_3 + y_4}{4}$$

e) For more precise calculation, the weighted centroid algorithm can then be calculated as:

$$x = \frac{\frac{x_1}{(d_A + d_B)} + \frac{x_2}{(d_B + d_C)} + \frac{x_3}{(d_A + d_C)}}{\frac{1}{(d_A + d_B)} + \frac{1}{(d_B + d_C)} + \frac{1}{(d_A + d_C)}} \quad (9)$$

$$y = \frac{\frac{y_1}{(d_A + d_B)} + \frac{y_2}{(d_B + d_C)} + \frac{y_3}{(d_A + d_C)}}{\frac{1}{(d_A + d_B)} + \frac{1}{(d_B + d_C)} + \frac{1}{(d_A + d_C)}}$$

Based on the above algorithms, the location of PD source was estimated. Flow chart of centroid and weighted centroid algorithms are shown in Figures 1 and 2 respectively.

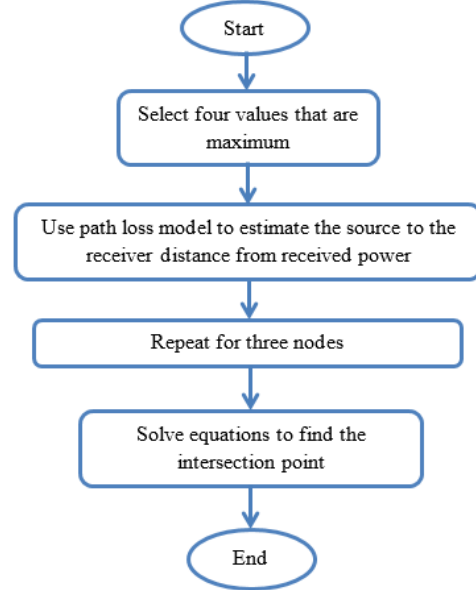


Figure 1. centroid algorithm flow chart.

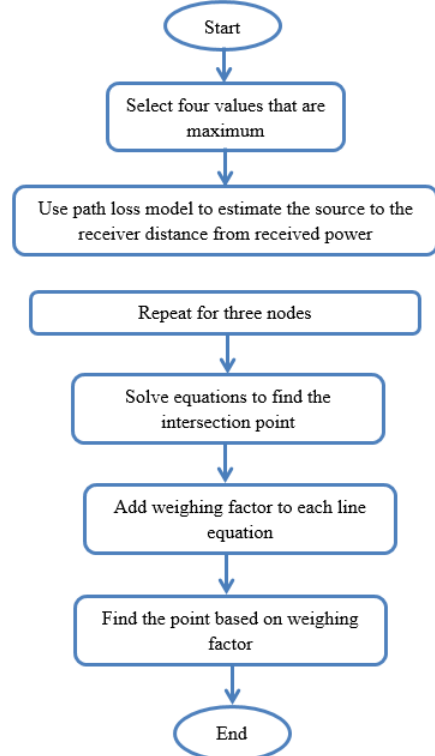


Figure 2. Weighted centroid algorithm.

#### IV. EXPERIMENTAL SETUP AND RESULTS

To check the performance of the algorithms, an artificial PD signal was generated and eight measurement sensors were used. To generate the PD signal an HVPD calibrator was used as shown in the Figure 3 below:

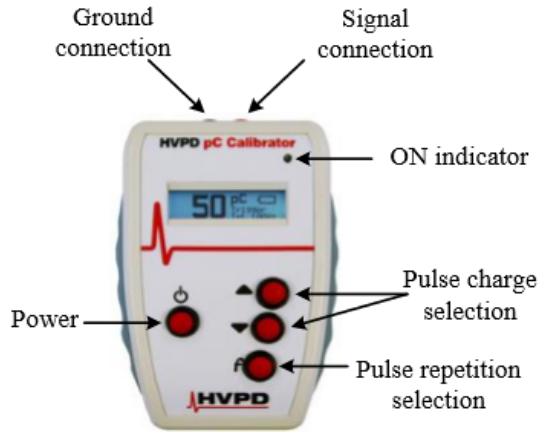


Figure 3. PD calibrator used for signal generation.

Sensors nodes were deployed for different configurations as shown in Figure 4 below:

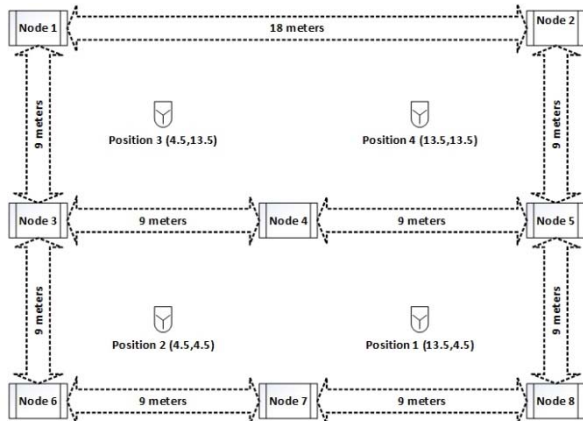


Figure 4. Sensors nodes deployment.

As shown in Figure 4, eight measurement nodes were used to perform the different measurements with source positioned at four different positions.

A PD signal of 10 nC was generated at 100 Hz repetition rate. A bi-conical antenna with the frequency range from 10MHz-1GHz was used and the calibrator was connected to the antenna. The antenna characteristics were measured by the manufacturer to provide the antenna factor of 16.5dB/m at the required frequency band. To measure the signal, RF sensors were used. RF sensor had parts including RF front end, microcontroller, and signal conditioning and communication unit. Three main parts of the RF front end include the RF filters, low noise amplifier and the envelope detector. The signal conditioning unit consists of the amplifier, comparator and the mono-stable circuits. The output from signal condition unit is fed into the microcontroller unit where analogue to digital conversion of the signal is performed as well. Wireless HART is utilized to send/receive data from one node to another, it is selected

among the other candidates due to its suitability in deployment under harsh industrial conditions. Figure 5 shows the experimental setup in a sports hall with measurement equipment used.

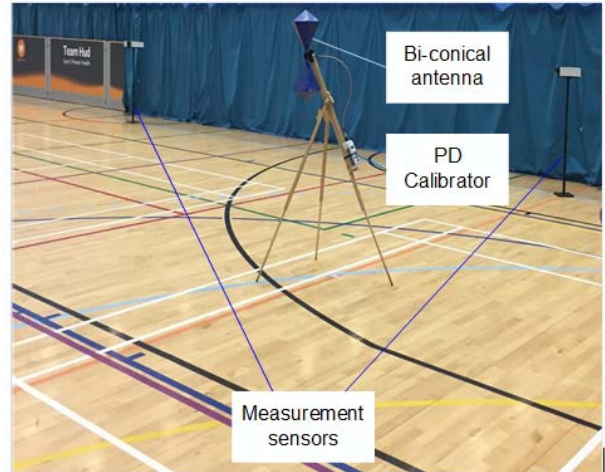


Figure 5. Experimental system

The results for all four positions are shown in Figures 6 and 7, 8 and 9 respectively.

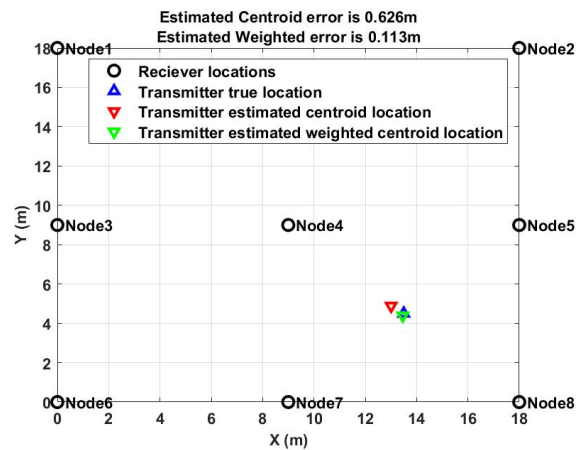


Figure 6. Position 1 estimated location.

It is evident that localisation error is below 1 meter using both algorithms.

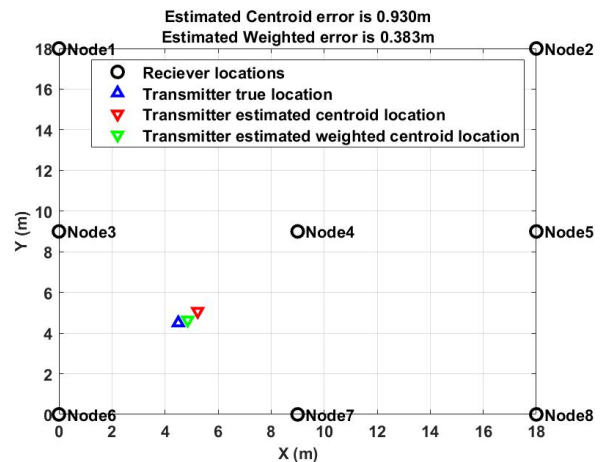


Figure 7 Position 2 estimated location

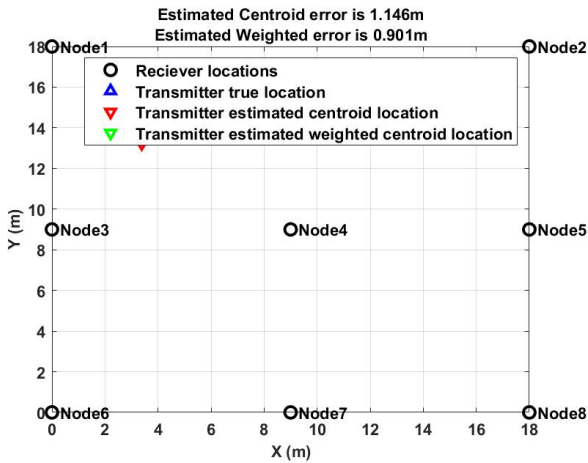


Figure 8. Position 3 estimated location.

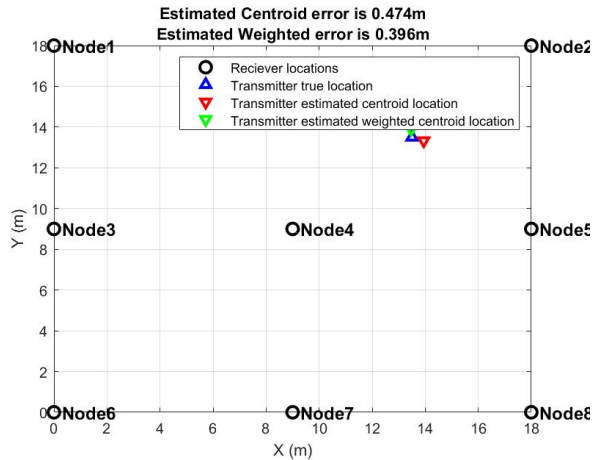


Figure 9. Position 4 estimated location.

The optimal and weighted centroid algorithm was applied on each measurement. It is important to note that the path loss exponent was set 2 for each measurement. It was observed that the centroid algorithm does not depend on the path loss exponent values therefore a default value was chosen.

## V. CONCLUSION

RSS based localization of a PD source for four different positions was performed using centroid and weighted centroid algorithms in an indoor environment. The results show that source estimation was possible. For all four positions, source location estimation showed an error around 1 meter or less. For all four positions, weighted centroid algorithm shows the localization error remains less than 1 meter. Centroid algorithm shows the localization error of 1.25 meters for position 2 and for all other positions, the error remains less than 1 meter. Considering the simplicity of the algorithms, the results achieved are satisfactory.

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