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1 Conservation management within strongholds in the face of disease-mediated invasions:
2 red and grey squirrels as a case study.

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20

21 Running title: Conservation faced with disease-mediated invasion

22

23

24 **Summary**

- 25 1. There is increasing evidence that disease-mediated invasions are widespread across a
26 range of vertebrate, invertebrate and plant systems. We therefore need a better
27 understanding of the role of disease in managing conservation threats due to introduced
28 and invasive species.
- 29 2. Here we develop a general theoretical model framework to assess the impact of
30 disease-mediated invasion on the viability of conserving native species through refuges
31 taking into account explicit spatial and stochastic processes.
- 32 3. The model techniques are applied to the well-documented red and grey squirrel
33 conservation system in the UK as a case study.
- 34 4. By combining general and specific modelling approaches we are able to make
35 management predictions while also gaining an understanding of the processes that
36 underlie population outcomes leading to more robust conservation practice.
- 37 5. Model results indicate that in the absence of control of the invading species, native
38 populations are driven to extinction both in the absence of disease (through
39 competition) and more rapidly when the disease is included (through competition and
40 disease processes).
- 41 6. When control is applied to reduce the abundance of the invading species there is a
42 threshold in the level of control, above which the invading population can be prevented
43 from establishing and the native species can be protected.
- 44 7. Highly virulent infections – squirrelpox in red squirrels – lead to periodic outbreaks of
45 disease in the native population due to continual invasion attempts from the disease-
46 carrying invader. Infections with low virulence may become established at endemic
47 levels in native populations. Therefore an important finding is that the disease can
48 spread through the native species even when the invading species is prevented from
49 establishing.
- 50 8. The benefits of increased density may be countered by an increased risk of disease
51 outbreaks. Therefore a critical message is that there is a correlation between native
52 density (and therefore habitat quality) and the impact of disease "harmful" to native
53 species.
- 54 9. Control of the invading species to prevent it establishing in strongholds can protect the
55 native species from exclusion, but may not protect it from disease outbreaks.
- 56 10. *Synthesis and applications.* Disease outbreaks in the absence of the invading species
57 can result in significant population crashes and therefore represents a serious threat
58 since it contributes to the risk of population extinction by suppressing the size of the
59 population making it more vulnerable to extinction through stochastic processes.
- 60

61 **Introduction**

62

63 Introductions and invasions of exotic organisms continue to cause significant damage to
64 native communities (Kolar & Lodge 2001). The rate at which human activity is introducing
65 species into new habitats is increasing (Prenter *et al.* 2004) and furthermore changes in
66 climate are likely to lead to significant and potentially rapid shifts in species ranges
67 (Rosenzweig *et al.* 2007). As a consequence the invasion and establishment of non-native
68 species are recognised as a major international threat to native biodiversity (Ruddock *et al.*
69 2007; Rosenzweig *et al.* 2007). Understanding the processes that determine successful
70 invasion is therefore a key challenge for ecological theory in order to underpin
71 conservation efforts and thereby sustain ecosystems and species communities
72 (Sutherland *et al.* 2006). Clearly there are likely to be many factors that determine the
73 success and rate of spread of invasive species but it is now recognised that shared
74 infectious disease is often a key determinant of invasive success (Daszak, Cunningham &
75 Hyatt 2000; Prenter *et al.* 2004; Strauss, White & Boots 2012). We therefore need a better
76 theoretical understanding of the role of disease in managing conservation threats due to
77 introduced and invasive species.

78

79 Typically when the role of parasites in invasions is discussed it is through their absence
80 since parasites along with predators and herbivores are key components of the “enemy
81 release hypothesis”, where the nonindigenous species gains an advantage because it
82 arrives in a new habitat without its natural enemies (for reviews see Wolfe 2002; Torchin &
83 Mitchell 2004). However, invasive organisms may also introduce diseases that can infect
84 native competitors leading to a “disease-mediated invasion” (Strauss, White & Boots
85 2012). There is increasing evidence across a range of vertebrate, invertebrate and plant
86 systems that such disease-mediated invasions are important determinants of invasion
87 success (Prenter *et al.* 2004; Strauss, White & Boots 2012). Well-known examples include,
88 (i) crayfish plague introduced with the invasive signal crayfish which has been responsible
89 for mass mortality in British white-clawed crayfish populations and poses a threat to native
90 crayfish species in Europe and Asia (Gherardi & Holdich 1999); (ii) the replacement of the
91 pedunculate oak in the UK by the introduced Turkey oak due to the impact of the knopper
92 gall wasp (Hails & Crawley 1991) and (iii) the expansion of the white-tailed deer in North
93 America into territories occupied by moose and caribou which has been aided by
94 macroparasitic meningeal worms carried by the white-tailed deer and which proved lethal

95 to the other species (Oates, Sterner & Boyd 2000). A recent review (Strauss, White &
96 Boots 2012) makes the case that disease-mediated invasions are a widespread
97 phenomenon in both plants and animals and may be particularly important in explaining
98 the replacement of native animals with phylogenically similar exotic species.

99

100 A key example of a disease-mediated native replacement is the invasion of grey squirrels
101 *Sciurus carolinensis* into the UK. Since its introduction into the UK in Victorian times, the
102 grey squirrel has replaced the native red squirrel *S. vulgaris* throughout most of England
103 and Wales, and in parts of Scotland and Ireland (Bryce 1997, O'Teangana 2000, Gurnell
104 *et al.* 2004). There are now only particular regions in which the red squirrel survives and
105 maintaining these populations is a major conservation priority (Ruddock *et al.* 2007; Parrott
106 2009). There is strong evidence both that grey squirrels are superior competitors in
107 habitats dominated by large-seeded deciduous tree species (Gurnell *et al.* 2004) and that
108 a shared virus, squirrelpox (SQPV), plays a critical role in red squirrel replacement. The
109 virus infects but is relatively avirulent to the greys yet is highly virulent to reds (Tompkins *et*
110 *al.* 2002; McInnes *et al.* 2006). Mathematical models suggest that while competition alone
111 can lead to the replacement of reds by greys, the inclusion of squirrelpox infection is
112 required to match the rapid replacement of red populations observed in the field
113 (Tompkins, White & Boots 2003). Importantly the models (Tompkins, White & Boots 2003)
114 show that the density of infected red squirrels is predicted to be low, despite the marked
115 effect on the population dynamics. This emphasises that low visibility of a disease does
116 not imply low importance of the disease and highlights the difficulty in observing infection
117 by virulent infectious diseases in the field. In the case of squirrelpox it took over 50 years
118 from the first observation of disease outbreaks in red squirrels (Middleton 1930) to the
119 identification of the virus (Scott, Keymer & Labram 1981) and a further 14 years before its
120 impact on red survival was suggested (Sainsbury & Gurnell 1995); culminating with the
121 current view that squirrelpox is unequivocally linked to the replacement of red squirrels and
122 a key threat to the species survival in the UK (Bosch & Lurz 2012).

123 Models have played an important role in highlighting the importance of the disease, but
124 they can also be used to help determine conservation management strategies in the face
125 of disease-mediated invasions. A key conservation strategy to protect endangered native
126 populations is the establishment of refuges or strongholds. These tend to be legally
127 protected areas that contain particular habitat types and/or management that favour the

128 threatened species when faced with threats that encompass environmental and land-use
129 change, habitat loss and degradation, disturbance, poaching, alien species and climate
130 change (e.g. Laurance *et al.* 2012, Demeke, Renfree & Short 2012). Well-known examples
131 include bamboo forests for mouse deer *Moschiola indica* in India (Ramesh *et al.* 2013);
132 sanctuaries for elephants *Loxodonta africana africana* in Ethiopia (Demeke, Renfree &
133 Short 2012) or strongholds that offer protection for endangered primates such as the drill
134 *Mandrillus leucophaeus* in Africa (Morgan *et al.* 2013). Since refuges play a key role in the
135 protection of endangered species from invasion and the impact of disease-mediated
136 invasion is increasingly recognised as a significant threat to native biodiversity (Strauss,
137 White & Boots 2012), it is important to assess the potential and limitations of the role
138 refuges or strongholds in the conservation of threatened native species.

139
140 In this study we develop a theoretical model framework to assess the impact of disease-
141 mediated invasion on the viability of conserving native species in refuges. The underlying
142 model system combines classical frameworks for modelling species interactions and
143 disease transmission and the results therefore provide critical information on the impacts
144 of preventative strategies and their likely consequences on alien–native–disease systems
145 in general. We examine in detail the well-documented red–grey squirrel conservation
146 system in the UK as a case study. Refuges (strongholds) have been employed in the UK
147 to conserve red squirrel populations. These strongholds are local forest regions that are
148 large enough to sustain viable red squirrel populations over the long-term, and in which
149 habitat composition and management offers native red squirrels a competitive advantage
150 over greys. Strongholds may be isolated from surrounding (grey squirrel) populations
151 (through poor connectivity or poor adjoining habitat) or grey squirrel density may be
152 controlled through trapping and removal (Anon. 2012). To date, there are 18 strongholds in
153 Scotland and 17 in the North of England managed by Government, Non-Government and
154 Charitable organisations (such as the Forestry Commission, Scottish Natural Heritage and
155 the Wildlife Trust). In addition, five red squirrel preferred areas (RSPAs) were identified in
156 Northern Ireland, and management for red squirrels in 'Focal Areas' is being implemented
157 in Wales (see Scottish strongholds: www.forestry.gov.uk/inf-d-7q3ft8; see also overall UK
158 strategy for all regions: www.forestry.gov.uk/fr/ukrsg). The general model framework was
159 parameterised to focus on the specific case study of the UK squirrel system. This allowed
160 an assessment of the effectiveness of management in terms of refuge habitat

161 characteristics and grey squirrel control on the outcome of red squirrel population survival.
162 The model framework was able to take into account the, often subtle, interactions between
163 individual species population dynamics, competition, the infectious disease and grey
164 squirrel control in strongholds. Overall our models give us insight into management within
165 strongholds in the face of disease-mediated invasions and can provide predictions of the
166 impact of specific control strategies in the UK red squirrel refuges.

167 The red–grey squirrel system represents a general framework for understanding the role of
168 disease-mediated invasion when the disease is highly virulent to the native species. The
169 general framework can also be modified to consider alternative disease characteristics and
170 we consider a parasite that has low virulence in the native species. By considering
171 different host densities in the refuge we alter the long-term reproductive ratio of the
172 disease (R_0) for both the high and low virulence cases and therefore capture a wide range
173 of host and parasite scenarios. In particular we contrast the impact of an acute highly
174 virulent parasite, such as squirrelepox, with that of a chronic low-virulence parasite.

175

176 **Materials and methods**

177 Our previous models on the impact of disease-mediated invasion have developed a
178 framework that combines the classical deterministic approaches in population ecology of
179 competition modelling and disease modelling to understand the role of competition and
180 shared disease in the replacement of red squirrels by greys (Tompkins, White & Boots
181 2003). The benefit of this modelling approach is that it provides a framework from which to
182 understand the influential mechanisms that arise between interacting populations, but the
183 disadvantage is that they cannot accurately assess the risk of invasion (since they do not
184 include the chance of extinction or disease fade-out at low density which may arise due to
185 stochasticity). In reality, invasions occur from low numbers and hence many attempts may
186 fail before establishment and successful invasion. Stochasticity has been included in rule-
187 based, spatially explicit models of the UK squirrel system (Rushton *et al.* 2000; 2006).
188 While these models have predictive power, it is difficult to isolate the key drivers of the
189 population dynamics due to the complicated choice of rules and large number of
190 parameters. The framework developed in this study falls between the deterministic and
191 rule-based approaches and will represent the stochastic nature of invasive spread and
192 success, but also allow the key mechanisms that drive the dynamics to be understood. As

193 such we can make relevant predictions while also gaining insight into the processes that
 194 underlie the outcomes.

195
 196 The model system represents the dynamics of native and invasive species and disease in
 197 a landscape of connected patches (see Figure 1, where we assume the stronghold is
 198 composed of a refuge and buffer zone). Within each patch the dynamics are represented
 199 by a stochastic version of the model of competition and disease developed by Tompkins,
 200 White & Boots (2003). Below we outline the model for the specific red–grey–squirrelpox
 201 system and later discuss how the results apply more broadly to disease-mediated invasive
 202 systems.

203
 204 The deterministic model of Tompkins, White & Boots (2003) where the dynamics of
 205 susceptible and infected red (S_R and I_R) and grey (S_G and I_G) squirrels and recovered
 206 (immune) greys (R_G) are represented by the following equations.

$$\begin{aligned}
 \frac{dS_G}{dt} &= (a_G - q_G (H_G + c_R H_R)) H_G - b S_G - \beta S_G (I_G + I_R) \\
 \frac{dI_G}{dt} &= \beta S_G (I_G + I_R) - b I_G - \gamma_G I_G \\
 \frac{dR_G}{dt} &= \gamma_G I_G - b R_G \\
 \frac{dS_R}{dt} &= (a_R - q_R (H_R + c_G H_G)) H_R - b S_R + \gamma_R I_R - \beta S_R (I_G + I_R) \\
 \frac{dI_R}{dt} &= \beta S_R (I_G + I_R) - b I_R - \alpha I_R - \gamma_R I_R
 \end{aligned} \tag{1}$$

209
 210 Here, $H_G = S_G + I_G + R_G$ and $H_R = S_R + I_R$ representing the total grey and red squirrel
 211 populations in each patch respectively. In Tompkins, White & Boots (2003) the two species
 212 have the same rate of adult mortality (b) but different rates of maximum reproduction
 213 (a_G, a_R) and different carrying capacities (K_G, K_R) which lead to susceptibilities to
 214 crowding (q_G, q_R) (since $q = (a - b)/K$). The competitive effect of grey squirrels on red
 215 squirrels is c_G , whilst that of red squirrels on grey squirrels is c_R . Squirrelpox virus is
 216 transmitted at the rate β both within and between each squirrel species with infected reds
 217 dying due to the disease at rate α , and infected greys recovering at rate γ_G (with reds
 218 recovering at rate γ_R when we consider general disease characteristics; $\gamma_R = 0$ for

219 squirrelpox). To generate the stochastic model, the rates in the deterministic model are
 220 converted to probabilities of events that account for changes in individual abundance
 221 within each patch (Renshaw 1991). The probabilities, P , of each event are determined as
 222 follows:

223

Birth of Grey to S_G	$P(S_G \rightarrow S_G + 1)$	$:[(a_G - q_G(H_G + c_R H_R))H_G]/R$	
Natural Death of S_G	$P(S_G \rightarrow S_G - 1)$	$:[bS_G]/R$	
Infection of Grey	$P(S_G \rightarrow S_G - 1, I_G \rightarrow I_G + 1)$	$:[\beta S_G(I_G + I_R)]/R$	
Natural Death of I_G	$P(I_G \rightarrow I_G - 1)$	$:[bI_G]/R$	
224 Recovery of Grey	$P(I_G \rightarrow I_G - 1, R_G \rightarrow R_G + 1)$	$:[\gamma_G I_G]/R$	(2)
Natural Death of R_G	$P(R_G \rightarrow R_G - 1)$	$:[bR_G]/R$	
Birth of Red to S_R	$P(S_R \rightarrow S_R + 1)$	$:[(a_R - q_R(H_R + c_G H_G))H_R]/R$	
Natural Death of S_R	$P(S_R \rightarrow S_R - 1)$	$:[bS_R]/R$	
Infection of Red	$P(S_R \rightarrow S_R - 1, I_R \rightarrow I_R + 1)$	$:[\beta S_R(I_G + I_R)]/R$	
Natural/Diseased Death of I_R	$P(I_R \rightarrow I_R - 1)$	$:[(b + \alpha)I_R]/R$	
Recovery of Red	$P(I_R \rightarrow I_R - 1, S_R \rightarrow S_R + 1)$	$:[\gamma_R I_R]/R$	

225
 226 In addition there are probabilities of individuals of each class moving to neighbouring
 227 patches. The probability of leaving the current patch for class S_G is

228

$$229 \quad P(S_G \rightarrow S_G - 1) : [mS_G F(H_G, H_R)]/R \quad (3)$$

230

231 here m is the long distance dispersal rate and $F(H_G, H_R) = (H_G + c_R H_R)^2 / (K_G)^2$ to represent
 232 saturation dispersal (Rushton *et al.* 2000) which reflects the situation in which squirrels are
 233 less likely to disperse when the absolute density in the grid patch is below the carrying
 234 capacity and more likely to disperse when above it. (Similar terms are used to represent
 235 dispersal in other classes.) In equations (2) and (3) $R = \sum [rates]$ (the sum of the terms in
 236 square brackets) and therefore transforms the rates to probabilities. We additionally
 237 specify the dispersal rate between the landscape and the buffer (Figure 1) as $p_m m$ where
 238 p_m is the proportional connectivity (such that when $p_m = 0$ the stronghold is isolated from
 239 the main landscape and when $p_m = 1$ the stronghold is connected with the same strength
 240 as the landscape patches). When an individual leaves a patch it enters a neighbouring
 241 habitable patch (see Fig. 1). We use the best estimate parameter set determined for the
 242 UK squirrel system as outlined in Tompkins, White & Boots (2003) and additionally define

243 $m = b$ to reflect that on average an individual is likely to undergo long distance dispersal to
244 a neighbouring patch once in its lifetime. These parameter values would lead to the
245 replacement of red squirrels by greys in the absence of disease (through competition) but
246 more rapid replacement when the disease is also included, see Tompkins, White & Boots
247 (2003). The parameters are also representative of a general parasite type that has high
248 virulence in the native species. In addition we consider alternative parasite types in which
249 the native species suffers low virulence ($\alpha = 2$) and in which R_0 is kept constant (by setting
250 $\gamma_R = 24$) to allow direct comparison between the high and low virulence scenarios. (A low
251 virulence parasite without recovery greatly increases R_0 and is considered in the
252 Supporting Information.)

253

254 The time between events is an exponentially distributed random variable and can be
255 determined as $T_{event} = -\ln(\sigma)/R$ where σ is a random number drawn from a uniform
256 distribution between 0 and 1 (see Renshaw 1991). The events are incremented at random
257 with the associated probabilities updated due to changes in population density after each
258 event. Individual simulations can be undertaken using a Gillespie algorithm and provide
259 information of the behaviour in a single realisation. Monte Carlo methods can be used to
260 generate multiple simulations to assess the average behaviour and variability across
261 realisations.

262

263 The spatial set-up is shown in Figure 1. Here the ring of linked patches (landscape
264 patches) is intended to represent the dynamics of the grey squirrel population that has
265 invaded and replaced the native reds (as is the case throughout much of England and
266 Wales). From one of these patches there is a connection to the buffer zone that surrounds
267 a refuge which is assumed to initially contain red squirrel populations. Management
268 strategies are employed in the buffer and refuge. This set-up approximates the situation in
269 strongholds where the protected red populations are surrounded by established grey
270 populations (such as many of the current strongholds in England; Parrott *et al.* 2009).

271

272 **Results**

273 *Baseline dynamics in the landscape and stronghold*

274 By considering high and low carrying capacity in the refuge and buffer zone we reflect the
275 impact of variation in habitat composition of different strongholds (Parrott *et al.* 2009) and

276 assess the influence of population density on disease-mediated invasion. The refuge and
277 buffer zone were initialised with red squirrels at their carrying capacity (in the absence of
278 disease). The landscape cells were initialised with grey squirrels at their carrying capacity
279 (when considering competition mediated invasion) or, when considering competition and
280 disease-mediated invasion, at the endemic equilibrium values determined from equations
281 (1) and assuming a squirrelpox prevalence of 74% (as in Tompkins, White & Boots 2003).
282 Test runs using 30 model simulations when there is no connection between the landscape
283 and buffer zone ($p_m = 0$) indicate that populations remain close to these initial conditions
284 with some fluctuation due to the stochastic nature of the simulations (Figures S1-S3).

285

286

287 *Dynamics in the stronghold in the absence of control*

288 When there is a connection between the buffer zone and the landscape cells, grey
289 squirrels can disperse into the buffer (and subsequently the refuge), compete with reds
290 and potentially transmit the infection. This leads to the exclusion of red squirrels from the
291 refuge with the dynamics and rate of replacement of reds dependant on the density in the
292 stronghold, the level of connection between the buffer and the landscape and whether the
293 disease is present.

294

295 When both the buffer and refuge have high carrying capacities the impact of disease is
296 marked and reduces the time to exclusion of reds (compared to the action of competition
297 alone) at all levels of connection between the stronghold and landscape (Figure 2a).
298 Dispersal of infectious greys from the landscape can trigger an epidemic in the red
299 population in the buffer with subsequent dispersal of infectious reds leading to an epidemic
300 in the refuge (Figure 2 b,c). Thus, the initial decrease in red abundance is due to a disease
301 epidemic in reds that occurs predominantly in the absence of grey invaders. This reduction
302 in the red population reduces the competitive pressure on greys, allowing them to increase
303 in number and subsequent disease outbreaks in reds and greys lead to further crashes in
304 the red population and their eventual exclusion. In the absence of disease, the
305 replacement process is significantly slower as the action of competitive replacement does
306 not result in dramatic crashes in red abundance (Figure 2 d,e). The time to exclusion
307 increases as the connection strength to the stronghold decreases (Figure 2a). In particular
308 when the connection is low, the chance of initial invasion is rare and it takes time before an

309 invasion is successful. This explains the increased variability in replacement time at low
310 levels of connectivity, which is particularly pronounced for disease-mediated replacement
311 since epidemics in the stronghold rely on rare dispersal events of infected individuals from
312 the surrounding landscape. Typical time series plots highlighting the variability in exclusion
313 times are shown in Figures S4-S6.

314

315 When carrying capacity is high in the refuge but low in the buffer zone the difference
316 between disease-mediated and competition-only replacement times can still be observed,
317 but is less marked (Figure 3a). Here the density of reds in the buffer zone is insufficient to
318 cause a disease outbreak until the density of greys has increased through competitive
319 replacement. Once an epidemic occurs in the buffer zone infection can spread to the
320 refuge causing a crash in red population abundance and accelerated replacement of reds
321 (Figure 3 b,c). In some simulations disease outbreaks fail to establish in the refuge and the
322 replacement process exhibits a similar pattern to that in the absence of disease (Figure 3
323 d,e).

324

325 When the refuge and buffer zone have low carrying capacities then there is no significant
326 difference between replacement times with and without the disease (Figure 4a). This is
327 because the disease does not cause an epidemic in red populations in either the low-
328 density refuge or buffer (Figure 4 b,c) and so replacement occurs through competition
329 processes only (see Figure 4 d,e). The time to exclusion is reduced for all levels of
330 connectivity compared to the high-density scenario (compare Figure 2a and 4a) simply
331 because it takes less time to outcompete an initially less abundant population.

332

333 When the chronic (low virulence) parasite type is considered the replacement times when
334 compared to the equivalent high-virulence scenarios is increased (Figure 5). Disease
335 outbreaks still occur and the disease can persist in the native population. However, the
336 reduced mortality from the disease means that the overall reduction in native abundance is
337 less marked and so replacement times lie between those reported for the highly virulent
338 parasite and the competition-only scenarios. A parasite type with low virulence and no
339 recovery has a greatly increased R_0 and here disease outbreaks lead to all native species
340 becoming infected (Figure S7). This disease type markedly reduces native abundance and
341 so the disease leads to a significant reduction in replacement times.

342

343 *Generality of results in the absence of control*

344 We have undertaken a range of simulations with different levels of high and low densities
345 in the stronghold and different densities in the landscape along with variations in the
346 disease and life history parameters and find results that are qualitatively similar to those
347 reported above under the assumption that the invader is a better competitor and the
348 disease is more harmful to the native species. When this assumption is suitably relaxed
349 the coexistence of native and invader or the exclusion of the invader is possible and so the
350 threat to the native species is reduced or removed and so is not a focus of this study (but
351 see Bell *et al.* 2009). Both the high and low virulence cases illustrate that the key driver of
352 disease-mediated replacement is for the disease to be sustained at endemic levels in the
353 landscape and for the density in the buffer and refuge to be sufficiently high to lead to
354 epidemics and population crashes within native populations. When the quality of the buffer
355 is poor it cannot support an epidemic outbreak, but rare dispersal of infected individuals
356 through the buffer can result in epidemics in the refuge and disease-mediated invasion.
357 When the disease cannot be supported in either the buffer or the refuge or if the disease is
358 absent, replacement occurs through competitive mechanisms only. Replacement is then
359 slower than when the disease has an impact.

360

361 *Dynamics in the stronghold with grey control*

362 We examined the effectiveness of control of grey squirrels as a strategy to protect and
363 maintain red squirrels in the refuge on the assumption that this may be necessary as
364 strongholds often contain habitat suitable for greys (e.g. Slaley Forest, in Northern
365 England, Parrott *et al.* 2009). Control was applied by removing a proportion, p_c , of greys
366 from the refuge and buffer at regular intervals (two control periods per year at six-month
367 intervals). Intensive removal followed by periods of monitoring and subsequent trapping is
368 a common field situation (for example see: www.snh.org.uk/pdfs/species/A260188.pdf).
369 Similar findings to those reported below occur if control is applied continually at a defined
370 rate or if control is applied whenever greys exceed a defined density. Figure 6 shows the
371 density of reds and greys in the refuge for different levels of control in the absence of
372 disease (Figure 6 a-c), with the disease characteristics of the squirrelpox (high virulence)
373 (Figure 6 d-f) and for the low-virulence disease scenario (Figure 6 g-i). There is a threshold
374 for the level of control above which red populations can be maintained in the refuge (which
375 can be visualised as the lowest level of control at which red squirrel abundance is

376 positive). This threshold level increases slightly as the connection between the stronghold
377 and the surrounding landscape increases, i.e. a higher level of control is required to
378 prevent red extinction as the connection strength increases (compare columns (i) and (ii)
379 in Figures 6). The threshold also increases as the abundance in the refuge decreases (it is
380 more difficult to protect a low-density refuge) with the threshold minimised for a high-
381 density refuge and low density buffer zone. There is little difference in this threshold level
382 for comparable parameters in the presence and absence of disease (compare Figure 6 a,
383 d and g, etc).

384

385 The main difference between the simulations with and without disease is that when the
386 disease is present the mean red abundance in the refuge is reduced and can show large
387 variability. This occurs as a result of disease outbreaks in the red populations in the refuge
388 (Figure 7 a-c) caused by the dispersal of infectious greys into the stronghold (that either
389 evade control or disperse between control events) that succeed in triggering an epidemic
390 in the red population in the buffer and refuge. For an epidemic to occur requires the
391 abundance in the refuge to be high. In the red–grey–squirrelpox system, control of greys
392 can prevent the exclusion of reds in the refuge but may not prevent periodic outbreaks of
393 the disease. When a disease outbreak occurs in the refuge it dramatically reduces the
394 population abundance (Figure 7 a,b) (since the disease is highly virulent to reds). This
395 reduced population level cannot support the disease in the long term leading to disease
396 fade-out. The red population can then recover to pre-infection levels since the control of
397 greys has removed or reduced the interspecific competitive pressure. Once red density
398 reaches a sufficiently high level the population it is once more prone to a disease outbreak
399 and therefore epidemics occur in the refuge periodically (Figure 7 a,b). When the density
400 in the buffer zone is low or the control level is high (which acts to lower grey density in the
401 buffer) or the connection between the stronghold and the landscape is low (compare
402 Figure 7 a and b) disease outbreaks in the refuge are less frequent.

403

404 The results with control of the invading species highlight key differences in the outcome of
405 disease-mediated invasion for different parasite types. In particular, while the highly
406 virulent infection produced periodic epidemics in the native species a low-virulence
407 infection may remain endemic in the native population (Figure 7d). This reduces the
408 density and variability of native species in the refuge (Figure 6 g(i) and g(ii)). Here, the
409 lower mortality of the parasite enables it to persist for longer periods, thereby reducing the

410 chance of disease fade-out, although for the disease to remain endemic re-infection from
411 the reservoir landscape population is still necessary. This is highlighted by comparing
412 Figure 7c in which buffer is at low density and so offers a poor connection to the reservoir
413 population, with the disease persisting over extended periods before fade-out, with Figure
414 7d in which the high-density population in the buffer enables the disease to remain
415 endemic in the refuge.

416

417 **Discussion**

418 Disease-mediated invasion is increasingly recognised as a key threat to biodiversity
419 (Prenter *et al.* 2004, Strauss, White & Boots 2012). As such, it may have important
420 consequences for the conservation and management of threatened native species within
421 refuges and other biological reserves. It is therefore essential to examine the ability of
422 conservation strongholds or refuges to maintain viable populations of native species in the
423 context of these disease-mediated invasions. By combining strategic and specific
424 modelling approaches it is possible make management predictions while understanding
425 the processes that underlie population outcomes leading to more robust conservation
426 practice. We discuss how our general model results provide insight into conserving native
427 species threatened by disease-mediated invasion, drawing on observations in the field.
428 Many of these observations relate to the red–grey–squirrelpox system as this has been
429 widely studied and protection of reds in strongholds is well established, but we stress that
430 the findings apply more generally.

431

432 In the absence of control of the invading species, native populations are driven to
433 extinction both in the absence of disease (through competition) and more rapidly when the
434 disease is included (through competition and disease processes). Therefore, in regions
435 where the invading species can outcompete the native species, control is required to
436 prevent replacement. An important general insight is that the presence of disease does not
437 have a significant impact on the threshold level of control required. However, while the
438 native species can be protected from replacement, disease outbreaks may be expected
439 due to continual invasion attempts from the disease carrying invader. Therefore a key
440 finding for both the high- and low-virulence parasite scenarios considered in this study is
441 that the disease can spread through the native species even when the invading species is
442 prevented from establishing (or at the onset of invasion), and here the results from our

443 stochastic model framework support those of spatial deterministic frameworks (Bell *et al.*
444 2009).

445

446 Disease outbreaks among the native population in the stronghold are most likely when the
447 population density is high and can result in significant population crashes. Disease
448 therefore represents a serious threat, since by suppressing the size of the population it is
449 more vulnerable to extinction through stochastic factors (Woodroffe 1999). Our general
450 predictions are supported by evidence from UK red squirrel strongholds. The high-density
451 red populations in Formby, Merseyside and in Whinfell, Cumbria have been protected by
452 trapping and removal of greys since the launch of strongholds in 2006 (Parrott *et al.* 2009),
453 but have suffered repeated outbreaks of squirrelpox which has resulted in a marked
454 reduction in population abundance, followed by disease fade-out and subsequent
455 population increases. A key message, therefore, is that control of the invading species to
456 prevent it establishing in strongholds can protect the native species from exclusion but
457 may not protect it from disease outbreaks, and therefore such epidemics should not be
458 seen as a failure in the control strategy (without control the native species would be rapidly
459 replaced through disease-mediated competition). Furthermore, wildlife managers employ a
460 number of strategies (e.g. supplemented feeding, habitat improvement) that may affect the
461 aggregation and density of target and non-target species with the unintended
462 consequence that parasites may also benefit (Cross *et al.* 2010). Our study highlights how
463 the benefits of increased density may be countered by an increased risk of disease
464 outbreaks. Therefore a critical message is that there is a correlation between native
465 density (and therefore habitat quality) and the impact of disease "harmful" to native
466 species.

467

468 This study highlights some general properties for the protection of native species in
469 strongholds. Intuitively, whenever possible strongholds should be chosen such that the
470 native species can outcompete the invader. For example, the Fleet basin stronghold (FCS
471 pers. Comm.) in the Galloway forest is composed predominantly of Sitka Spruce, which
472 supports low-density red squirrel populations but not greys (although greys are supported
473 in the surrounding better quality habitat). Here, either no or limited control is required at the
474 stronghold margins to prevent spillover from adjacent grey populations (FSC pers. comm.).
475 The low density of reds may also preclude widespread epidemic outbreaks (although
476 localised infection may occur at the interface between red and grey populations). The red

477 squirrel stronghold on the Isle of Arran and the red squirrels on the Isle of Wight are not
478 connected to mainland populations and can therefore support high-density red populations
479 in the long term (Lurz 2012). Nevertheless, monitoring should be undertaken and where
480 necessary contingency plans should be invoked to control and exclude 'accidental'
481 invasions and to limit potential disease risk. In connected strongholds where the disease-
482 carrying invader can outcompete the native species a continual control strategy would
483 have to be applied to prevent native replacement. Where the native species can be
484 supported at sufficiently high density, periodic disease outbreaks for highly virulent
485 parasites or persistence of the disease for low-virulence parasites would be expected and
486 may be difficult to prevent. A consequence of disease outbreaks is that it presents the
487 opportunity for the native species to develop immunity, which cannot develop without
488 control as the native is replaced through competition. In a few instances reds have been
489 shown to display antibodies to SQPV implying they have survived the infection (Sainsbury
490 *et al.* 2008). Testing in stronghold sites that exhibit disease outbreaks would provide key
491 evidence of the potential for the development of immunity to SQPV in red squirrels.

492

493 Our study highlights key differences in the way different parasite characteristics impact
494 native species threatened by disease-carrying invaders. Highly virulent diseases cause
495 severe population crashes in native species that hasten their replacement by invaders. For
496 instance, the monogenean gill fluke introduced by the Starry sturgeon to the Aral Sea
497 decimated native bastard sturgeon (Pourkazemi 2006), and over half of the native
498 Hawaiian bird species have gone extinct due to exposure to avian malaria and birdpox
499 spread by introduced, domestic birds (Warner 1968; van Riper *et al.* 1986). However, the
500 severity and short-lived nature of infection means the disease cannot be supported in
501 native populations and fade-outs leading to population recovery to pre-infection levels can
502 occur if the invading species is excluded (as observed for squirrelpox in red strongholds
503 (Parrott *et al.* 2009)). In contrast, our study indicates that introduced disease with low
504 virulence (with equivalent R_0 to the high virulence parasite), can remain endemic within
505 native species. This may explain why squirrel Adenovirus that is less virulent than SQPV,
506 but can cause mortality when associated with other stress factors, has been reported in
507 natural red squirrel populations that are free from grey squirrels with the disease persisting
508 for many years (Martinez-Jiminez *et al.* 2011; Everest *et al.* 2014). Other examples include
509 the persistence of the trypanosome parasite *Crithidia bombi* in native honeybees which
510 inhibits an infected individual's ability to search for nectar and can lead to death through

511 starvation. *Crithidia bombi* is spread from commercial honeybees used in greenhouses
512 with highest disease incidence in native species near greenhouses (Otterstatter &
513 Thomson, 2008; Meeus *et al.* 2011). Similarly, the amphibian chytrid fungus
514 *Batrachochytrium dendrobatidis* has emerged and spread through native amphibian
515 populations worldwide introduced by invading frog species. The virulence levels of disease
516 is species dependent but it can persists in some native species which then facilitates the
517 replacement of more susceptible species by resistant invaders (Akmentins &
518 Cardozo,2010; Kilpatrick, Briggs & Daszak 2010).

519

520 Our study has highlighted the impact that disease-carrying invaders can have on
521 replacement of native species and critically emphasised the difficulties in preventing
522 disease outbreaks when attempting to conserve threatened species. We suggest that
523 modelling frameworks that can represent the stochastic nature of invasive spread and
524 simulate disease dynamics can bridge a gap between our understanding of the risk from
525 invading species and the consequences of conservation management on the ground
526 (Joseph *et al.* 2013).

527

528

529 **Data accessibility**

530 This paper contains no new data.

531

532 **Supporting Information**

533 Additional supporting information may be found in the online version of this article:

534

535 Appendix S1. Baseline results and further simulations.

536

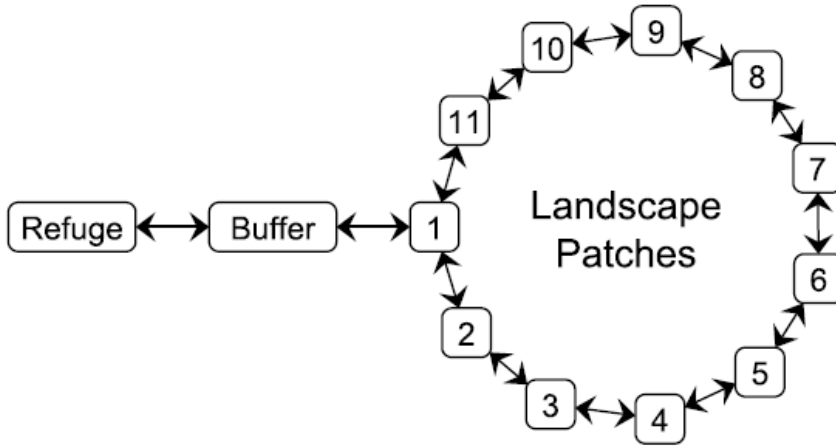
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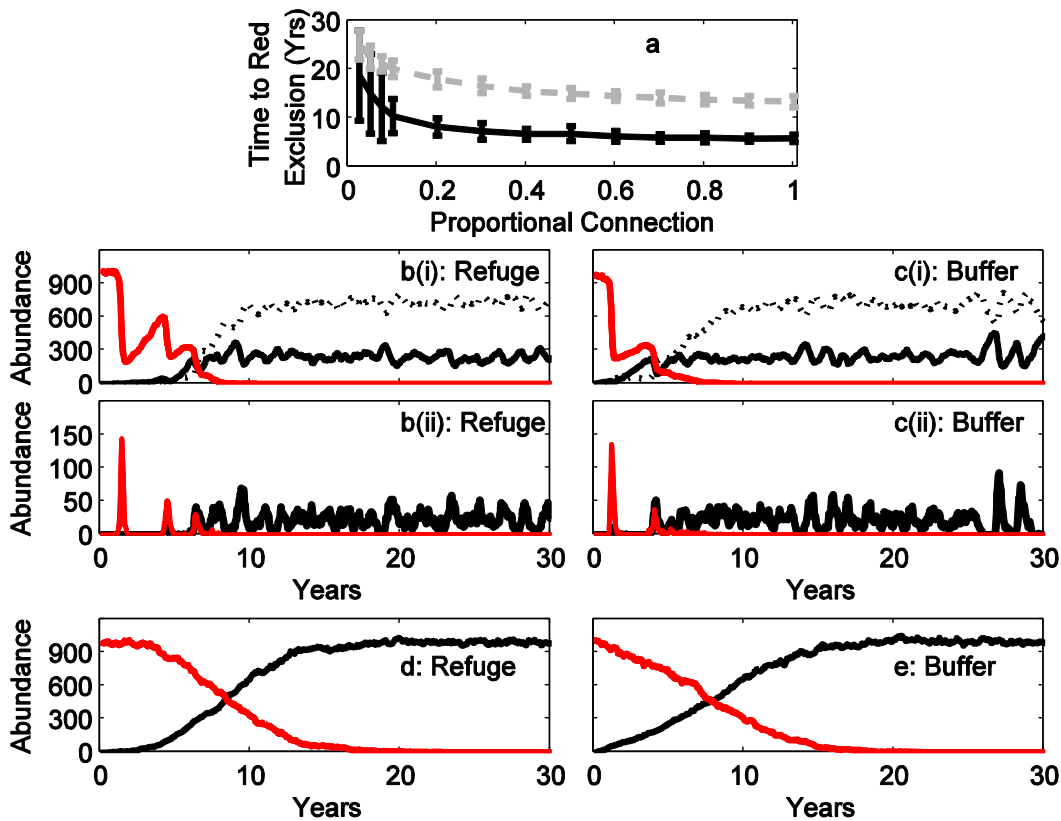


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Figure 1: Landscape patches are linked to neighbours in a ring and these are linked to a buffer zone and refuge (which together form the stronghold). The stochastic model, equations (2) and (3) represents the dynamics in each patch. Dispersal occurs to neighbouring patches as indicated by the arrows.

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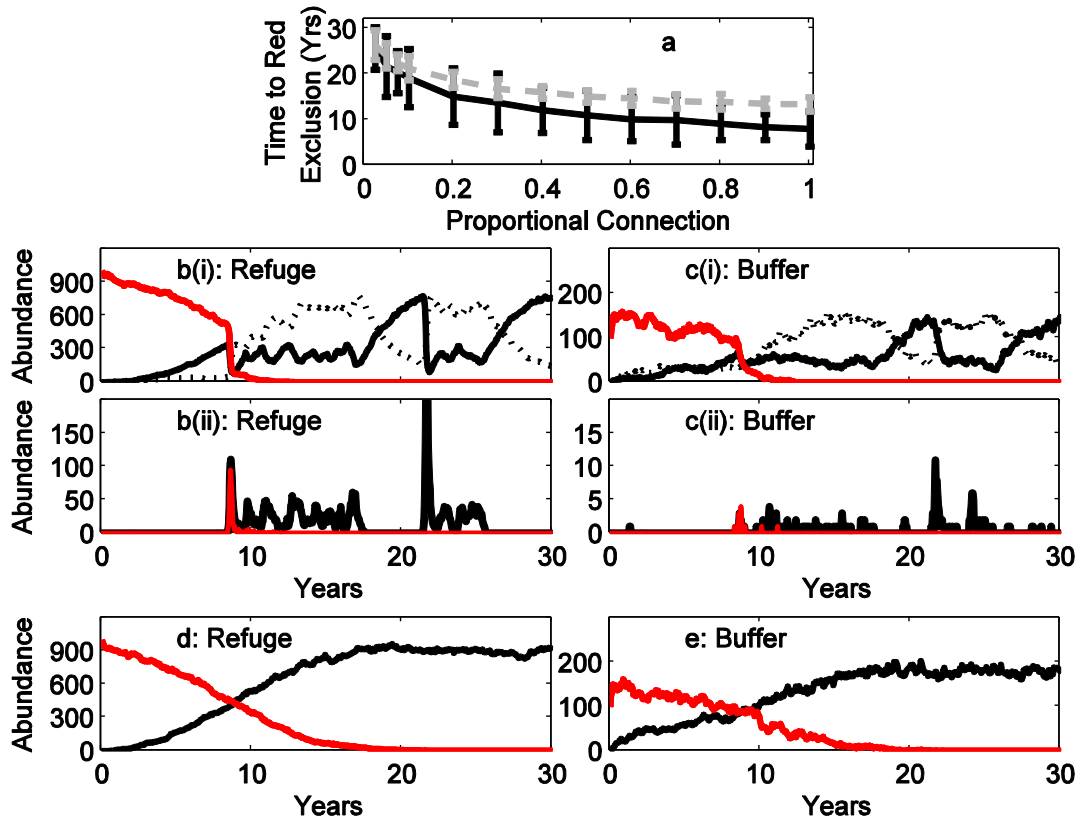


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667 Figure 2. Time to exclusion and population time series for parameters that represent squirrelpox
 668 (high virulence) when the carrying capacity for red and grey squirrels is high (1000) in the refuge
 669 and buffer zone. In (a) the time to exclusion of red squirrels in the refuge is plotted against the
 670 proportional level of connection between the landscape and buffer zone. The solid line represents
 671 the mean time to extinction (from 30 simulations, with 95% confidence intervals) when the disease
 672 is at endemic levels in the landscape patches and the dashed grey line when the disease is absent.
 673 Time series plots of population abundance (with proportional connection, $p_m = 0.2$) showing
 674 disease-mediated replacement in (b) the refuge and (c) the buffer zone are shown for (i) susceptible
 675 reds (red line), susceptible greys (black line) and recovered greys (dotted line) and (ii) infected
 676 reds (red line) and infected greys (black line). Time series plots for competition (only) replacement
 677 are shown in (d) the refuge and (e) the buffer zone for red squirrels (red line) and greys (black line).
 678 Parameters are as in Tompkins, White & Boots (2003) which are: $a_G = 1.2$, $a_R = 1.0$, $b = m = 0.4$,
 679 $\alpha = 26$, $\gamma_G = 13$, $\gamma_R = 0$, $\beta = 0.056$ the carrying capacity in the refuge and buffer are stated above
 680 and in the landscape, $K = 1000$.

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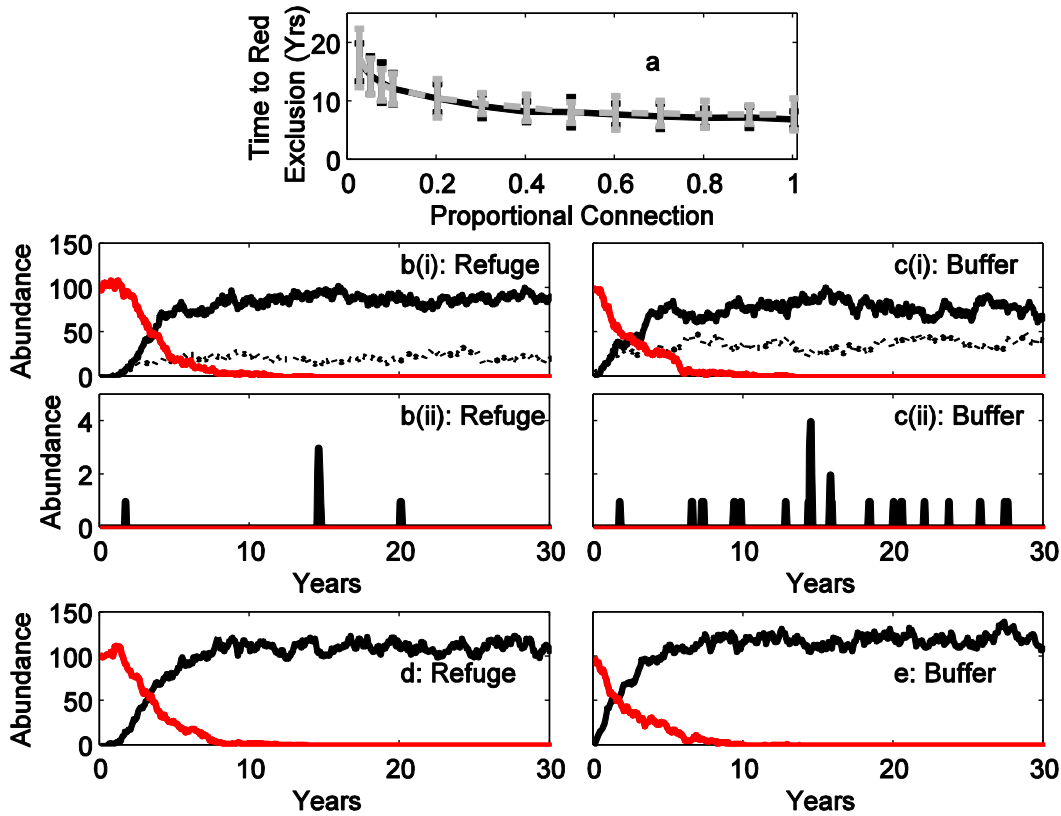
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685 Figure 3. Time to exclusion and population time series for parameters that represent squirrelpox
 686 (high virulence) when the carrying capacity for red and grey squirrels is high (1000) in the refuge
 687 and low (100) in the buffer zone. In (a) the time to exclusion of red squirrels in the refuge is plotted
 688 against the proportional level of connection between the landscape and buffer zone. The solid line
 689 represents the mean time to extinction (from 30 simulations, with 95% confidence intervals) when
 690 the disease is at endemic levels in the landscape patches and the dashed grey line when the disease
 691 is absent. Time series plots of population abundance (with proportional connection, $p_m = 0.2$)
 692 showing disease-mediated replacement in (b) the refuge and (c) the buffer zone are shown for (i)
 693 susceptible reds (red line), susceptible greys (black line) and recovered greys (dotted line) and (ii)
 694 infected reds (red line) and infected greys (black line). Time series plots for competition (only)
 695 replacement are shown in (d) the refuge and (e) the buffer zone for red squirrels (red line) and greys
 696 (black line). Other parameters are as in Figure 2.

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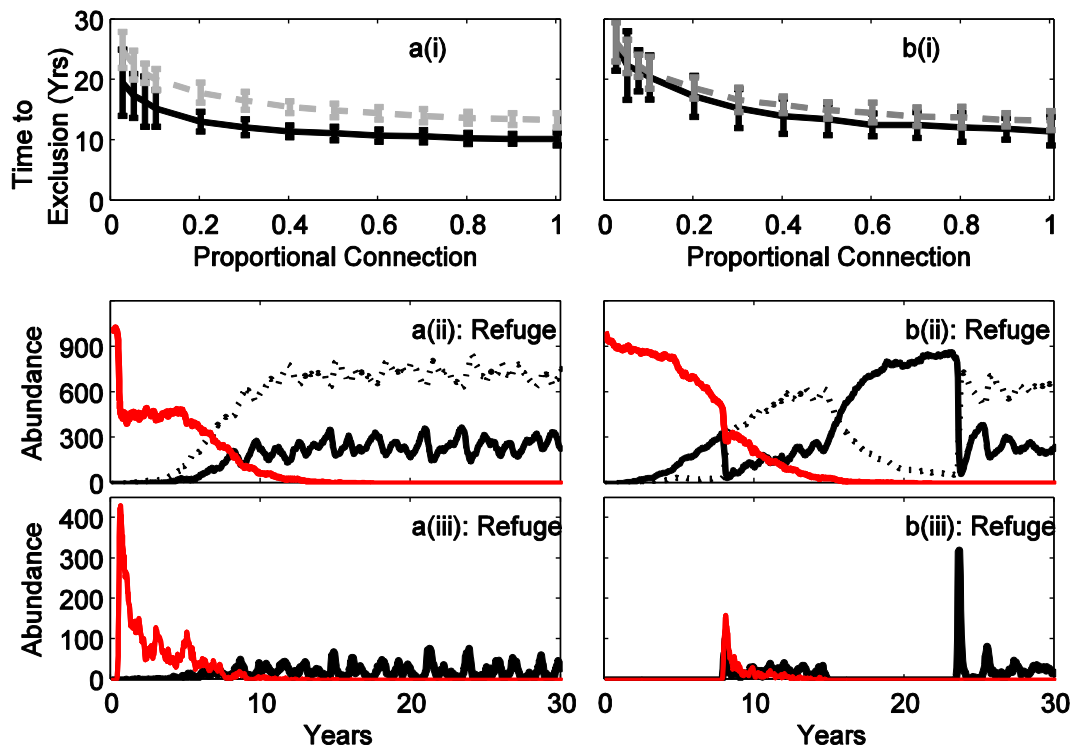
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702 Figure 4. Time to exclusion and population time series for parameters that represent squirrelpox
 703 (high virulence) when the carrying capacity for red and grey squirrels is low (100) in the refuge and
 704 low (100) in the buffer zone. In (a) the time to exclusion of red squirrels in the refuge is plotted
 705 against the proportional level of connection between the landscape and buffer zone. The solid line
 706 represents the mean time to extinction (from 30 simulations, with 95% confidence intervals) when
 707 the disease is at endemic levels in the landscape patches and the dashed grey line when the disease
 708 is absent. Time series plots of population abundance (with proportional connection, $p_m = 0.2$)
 709 showing disease-mediated replacement in (b) the refuge and (c) the buffer zone are shown for (i)
 710 susceptible reds (red line), susceptible greys (black line) and recovered greys (dotted line) and (ii)
 711 infected reds (red line) and infected greys (black line). Time series plots for competition (only)
 712 replacement are shown in (d) the refuge and (e) the buffer zone for red squirrels (red line) and greys
 713 (black line). Other parameters are as in Figure 2.

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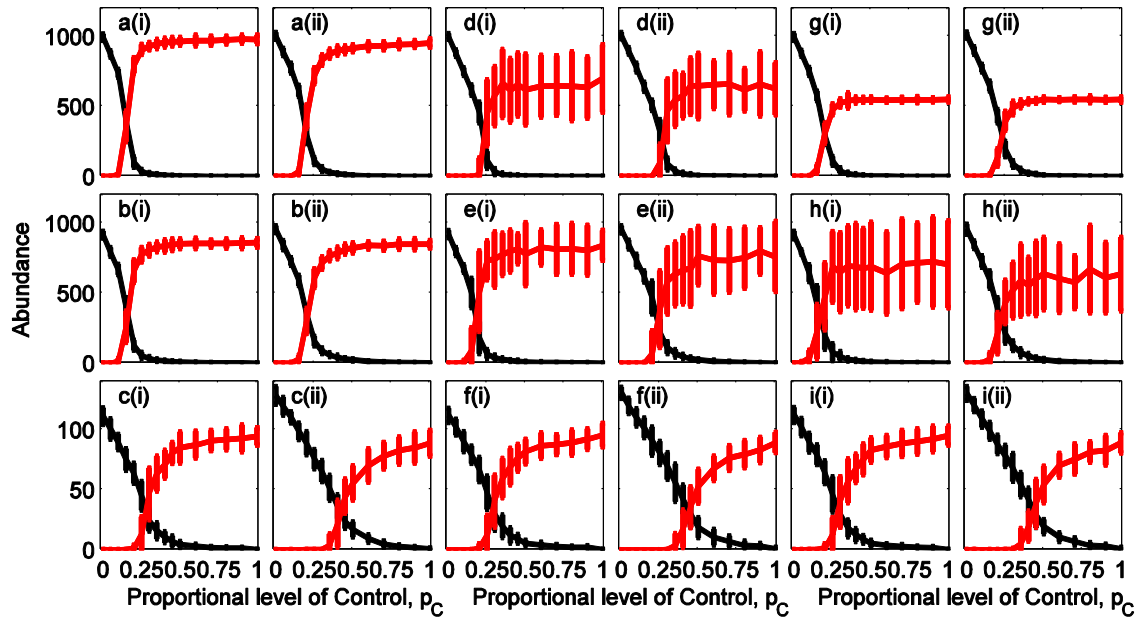
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718 Figure 5. Time to exclusion and population time series for parameters representing a parasite type
 719 with low virulence ($\alpha = 2$, $\gamma_R = 24$). The carrying capacity for the native and invading species is
 720 high (1000) in the refuge and in (a) high (1000) in the buffer zone and (b) low (100) in the buffer
 721 zone. In (i) the time to exclusion of native species in the refuge is plotted against the proportional
 722 level of connection between the landscape and buffer zone. The solid line represents the mean time
 723 to extinction (from 30 simulations, with 95% confidence intervals) when the disease is at endemic
 724 levels in the landscape patches and the dashed line when the disease is absent. Time series plots of
 725 population abundance (with proportional connection, $p_m = 0.2$) showing disease-mediated
 726 replacement in the refuge are shown for (ii) susceptible natives (red line), susceptible invaders
 727 (black line) and recovered invaders (dotted line) and (iii) infected natives (red line) and infected
 728 invaders (black line). Other parameters are as in Figure 2.

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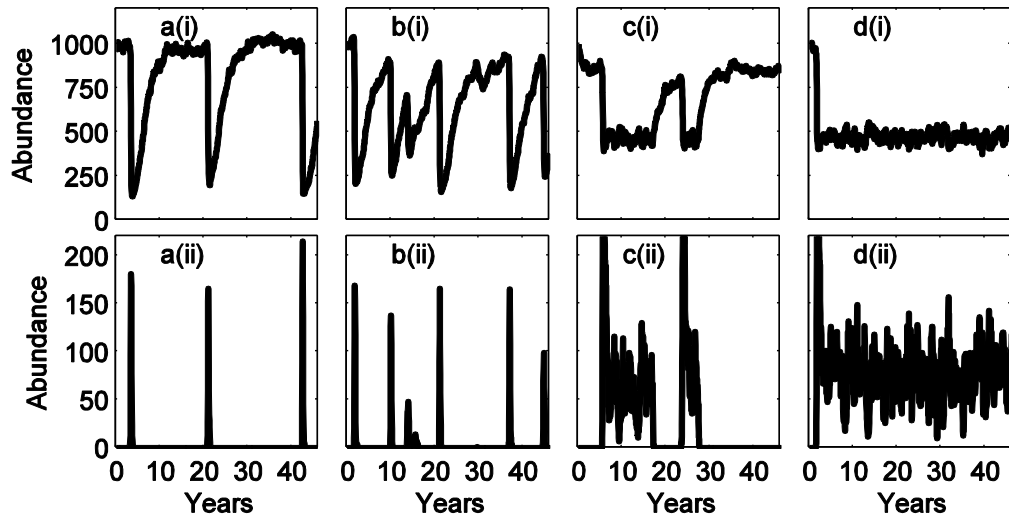
734 Figure 6: The average density (with 95% confidence intervals) in the refuge after 40 years where in
 735 plots (a-c) the parasite is absent in (d-f) the parasite has the properties of squirrelpox (high
 736 virulence) ($\alpha = 26$, $\gamma_R = 0$) and in (g-i) the parasite has low virulence ($\alpha = 2$, $\gamma_R = 24$) for
 737 red/native (red line) and grey/invading (black line) squirrels/species plotted against the proportional
 738 level of control of greys/invaders. Control is applied twice per year and removes the specified
 739 proportion of greys/invaders from the refuge and buffer zone. The proportional connection between
 740 the stronghold and the landscape is (i) $p_m = 0.2$ and (ii) $p_m = 1$ and the carrying capacities are
 741 (a,d,g) 1000 in the refuge and buffer, (b,e,h) 1000 in the refuge and 100 in the buffer, (c,f,i) 100 in
 742 the refuge and buffer. Other parameters are as in Figure 2.

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749 Figure 7: Time series for the population abundance of (i) susceptible reds/natives and (ii) infected
750 reds/natives in the refuge for a proportional control level, $p_c = 0.5$. In (a,b) the carrying capacity in
751 the refuge and buffer is high (1000) and the parasite has parameters representative of squirrelpox
752 (high virulence) ($\alpha = 26$, $\gamma_R = 0$). In (a) the proportional connection $p_m = 0.025$ and in (b)
753 $p_m = 0.2$. In (c,d) the parasite has low virulence ($\alpha = 2$, $\gamma_R = 24$) and the proportional connection
754 to the buffer $p_m = 0.2$. In (c) the carrying capacity in the refuge is high (1000) and in the buffer is
755 low (100) and in (d) the carrying capacity in the refuge and buffer is high (1000). Other parameters
756 are as in Figure 2.

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